

# Modeling Foraminifera in Framsticks. Genotype, phenotype, ecosystem

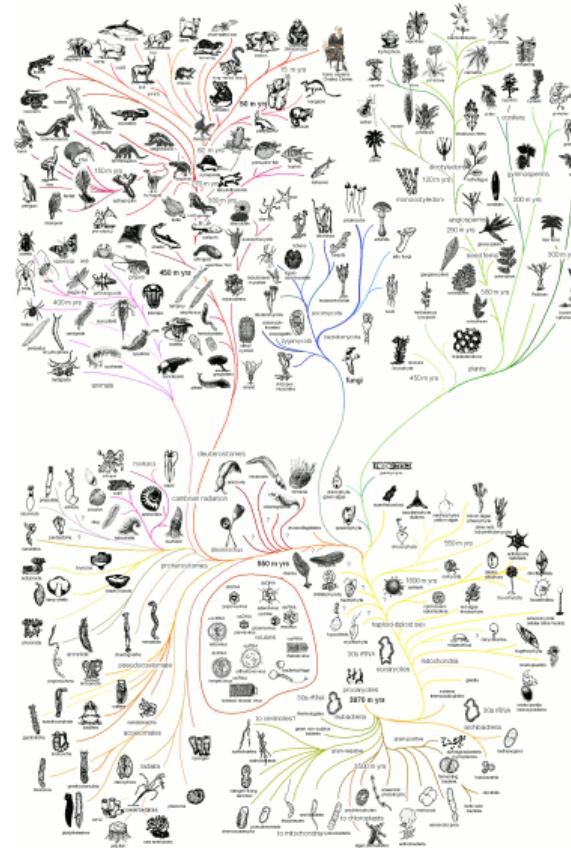
Maciej Komosinski   Agnieszka Mensfelt

[www.framsticks.com](http://www.framsticks.com)

Details of this research are available in [Kom+16; Kom+17]  
and at [www.framsticks.com/foraminifera](http://www.framsticks.com/foraminifera).

# Foraminifera in the Tree of Life

- Foraminifera
- Genotype-to-phenotype mapping
- Similarity measure
- Life cycle
- Population dynamics
- Conclusions
- References



# What are Foraminifera?

Foraminifera

Genotype-to-phenotype mapping

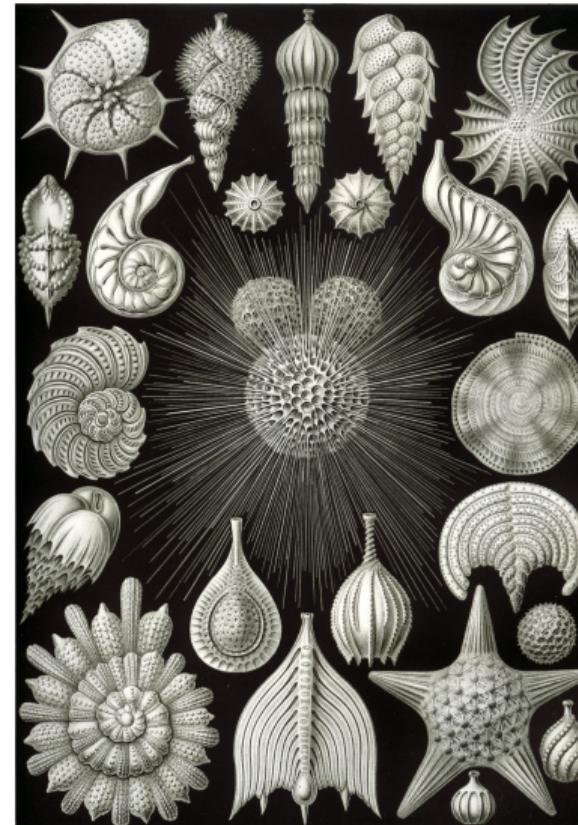
Similarity measure

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Ernst Haeckel, *Kunstformen der Natur*, 1904.

# What are Foraminifera?

Foraminifera

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Foraminifera in the Indian Ocean, Southeast Coast of Bali. Field width = 5.5 mm.  
Microphotographie personnelle by Psammophile.

# What are Foraminifera?

Foraminifera

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Tests of foraminifera extracted sand from the beach of Ngapali (Myanmar).  
Microphotographie personnelle by Psammophile.

# What are Foraminifera?

Foraminifera

Genotype-to-phenotype mapping

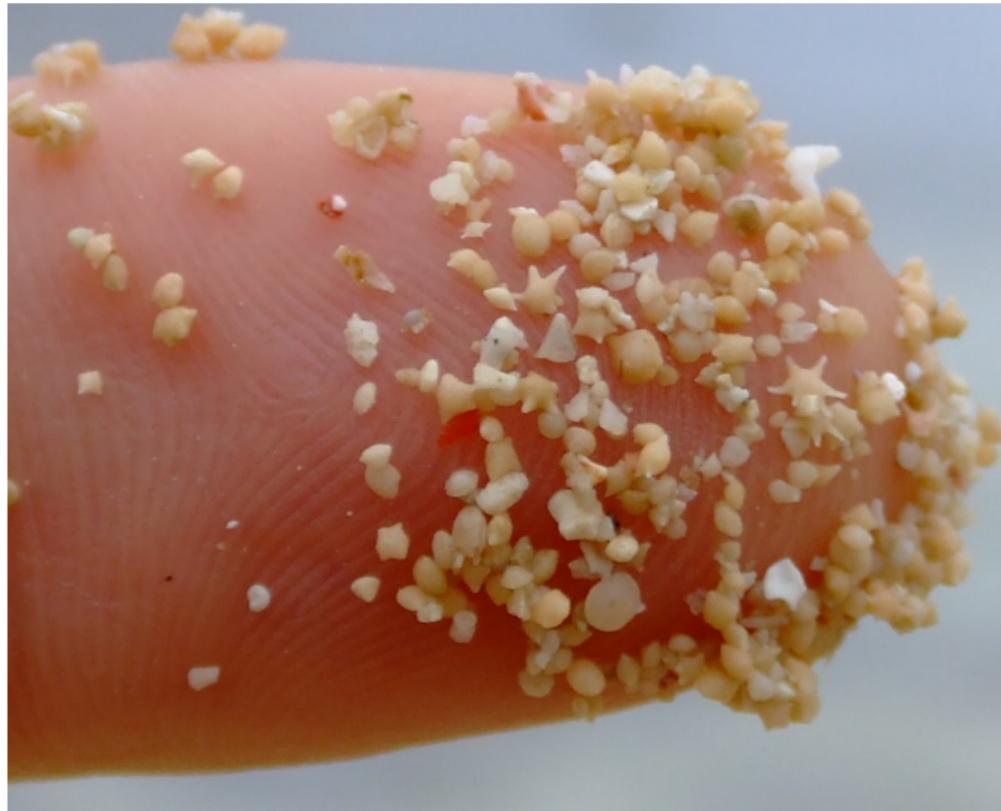
Similarity measure

Life cycle

Population dynamics

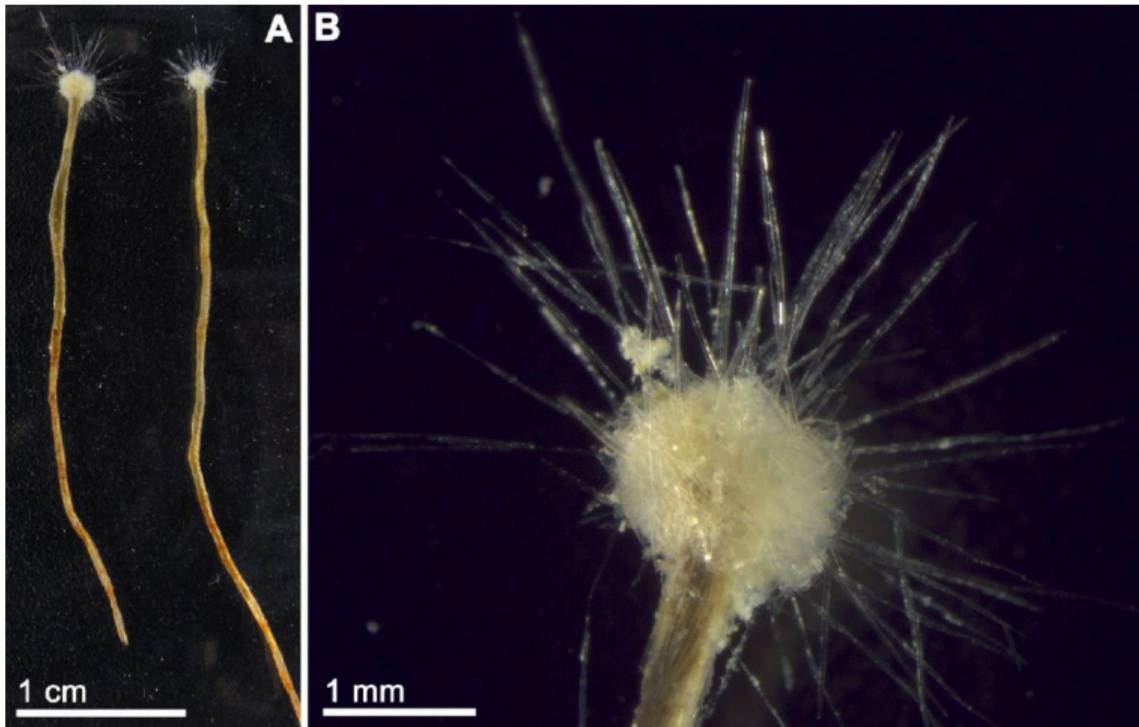
Conclusions

References



Star sand on Hoshizuna-no-hama, Iriomote, Okinawa.  
Own work by Geomr.

# What are Foraminifera?



Spiculosiphon oceana, a species of giant foraminiferan from the Mediterranean Sea. (A) General view of the holotype and the paratype (from left to right, respectively) of *Spiculosiphon oceana*. (B) Detail of capitate region of the holotype, showing the globelike, central structure and the radiating tracts of spicules.

A giant foraminifer that converges to the feeding strategy of carnivorous sponges. Zootaxa 3669 (4): 571–584. doi:10.11646/zootaxa.3669.4.9

Foraminifera

Genotype-to-phenotype mapping

Similarity measure

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# Motivations: why Foraminifera?

Foraminifera

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- single-celled organisms
- abundant as fossils for the last 540 million years (since the earliest Cambrian)
- diverse morphologies, from 100 micrometers to 20 centimeters
- catch their food with a network of thin pseudopodia
- 4,000 species: 40 species are planktonic (float in the water), others are benthic (bottom of the ocean)
- applications: biostratigraphy, paleoclimatology, paleoceanography, bioindicators, oil exploration
- much of our current knowledge about climate and past history of Earth comes from studies of foraminifera

# Goal: multiscale model

Foraminifera

Genotype-to-phenotype mapping

Similarity measure

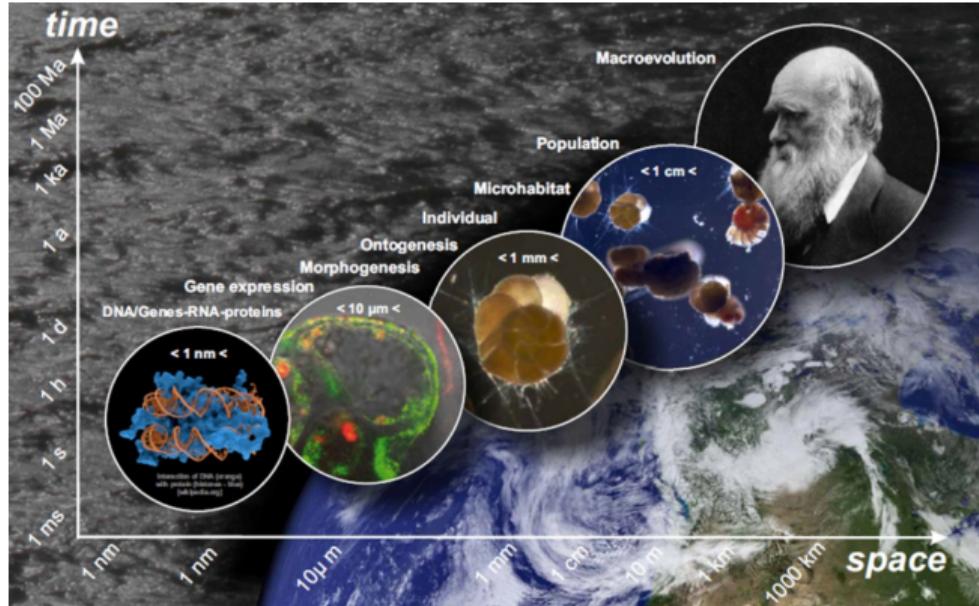
Life cycle

Population dynamics

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- multiple scales of time and space



- integration of existing knowledge on foraminiferal physiology and ecology, following qualitative and quantitative approaches
- testing hypotheses on different levels and asking questions!

# Genotypes and phenotypes

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$X(XX, RX(X, X))$

//3

5

aakyaabzakvzaabzdyzzxyabcdforwizehaaaaabhzz

//0

p:sh=2,sx=0.6,sy=0.6,sz=0.3,z=3.4,vr=0.8,0.8,0.4

p:sh=2,sx=0.1,sy=0.1,sz=0.1,vr=0.8,0.8,0.4

p:sh=2,sx=0.1,sy=0.1,sz=0.1,vr=0.8,0.8,0.4

j:0,1,sh=1,dx=0.45,dy=0.45,dz=-0.4

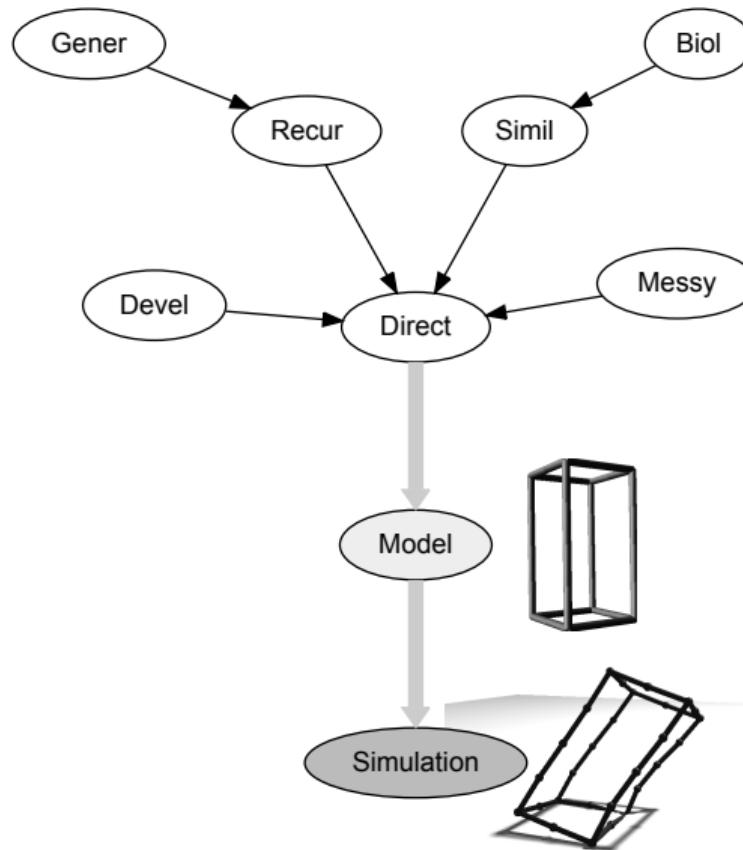
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...



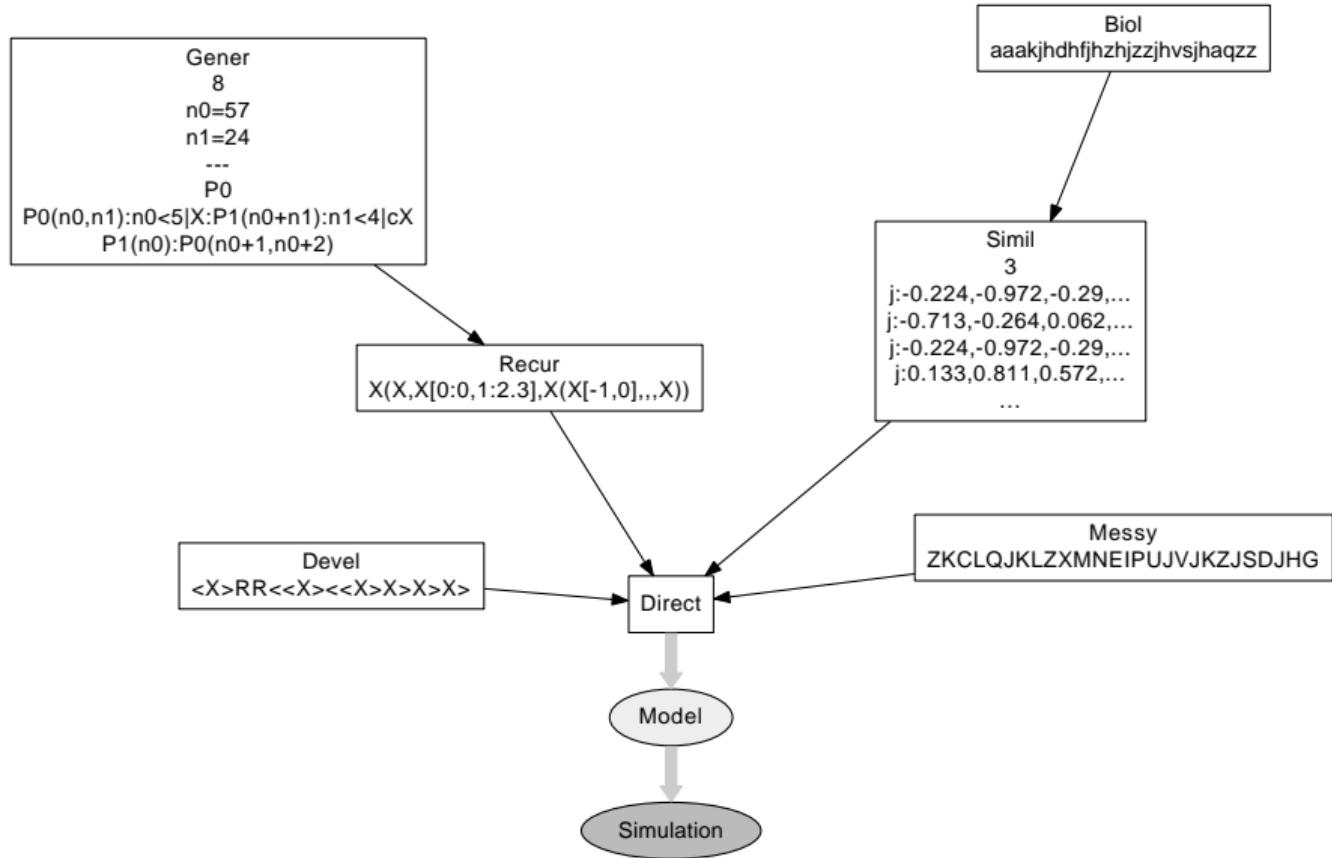
# The hierarchy of genetic encodings in Framsticks

- Foraminifera
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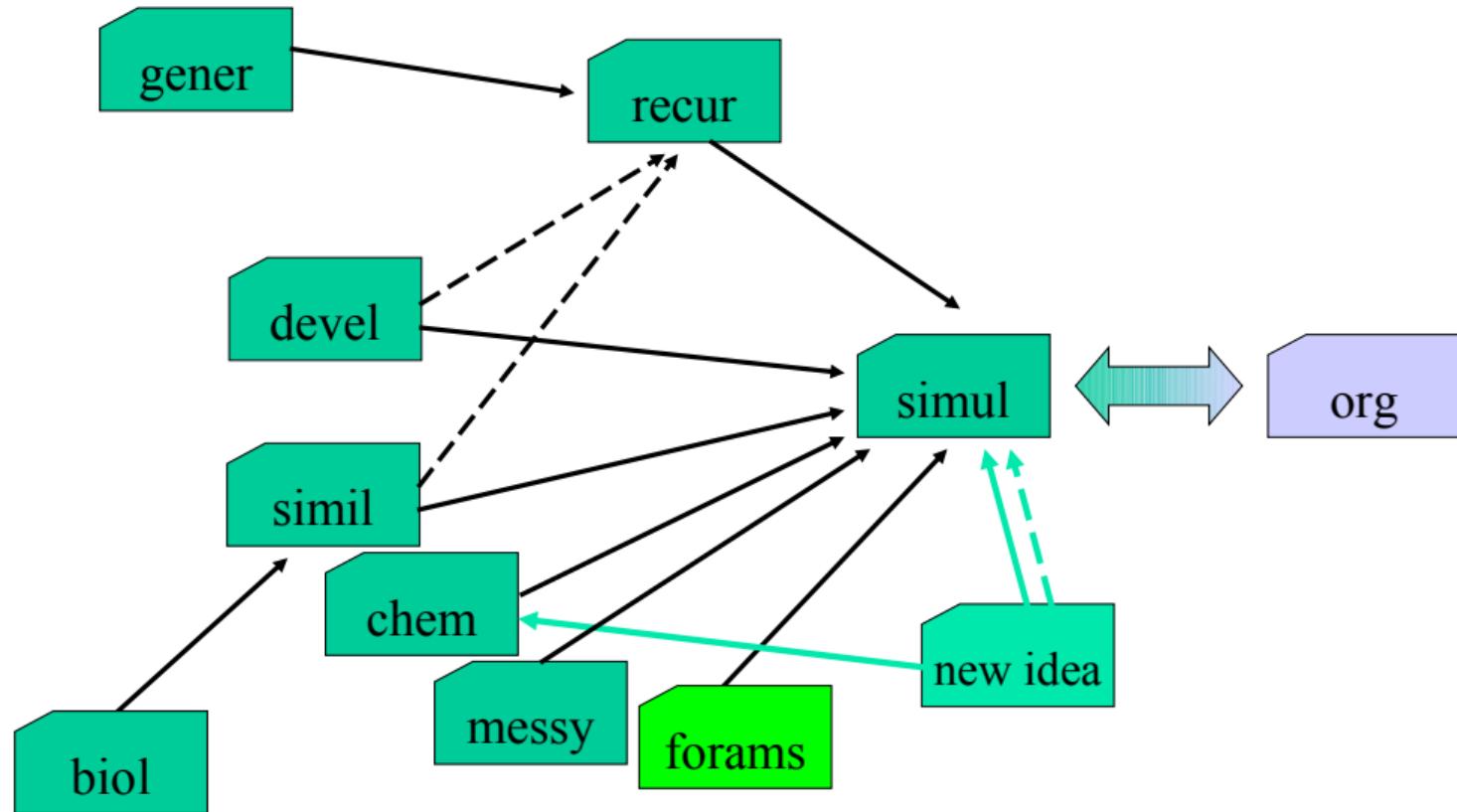
# Specialized genetic operators for each genetic encoding

Foraminifera  
Genotype-to-phenotype mapping  
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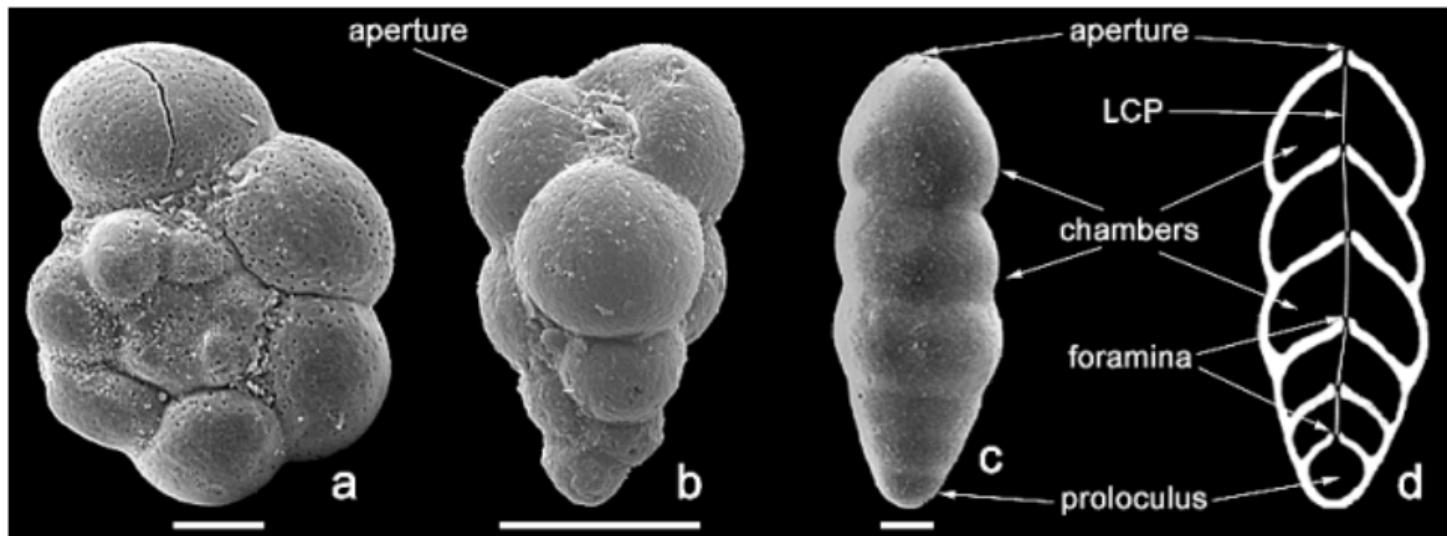
# Adding foraminiferal genetics to Framsticks

Foraminifera  
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References



# Foraminifera morphology

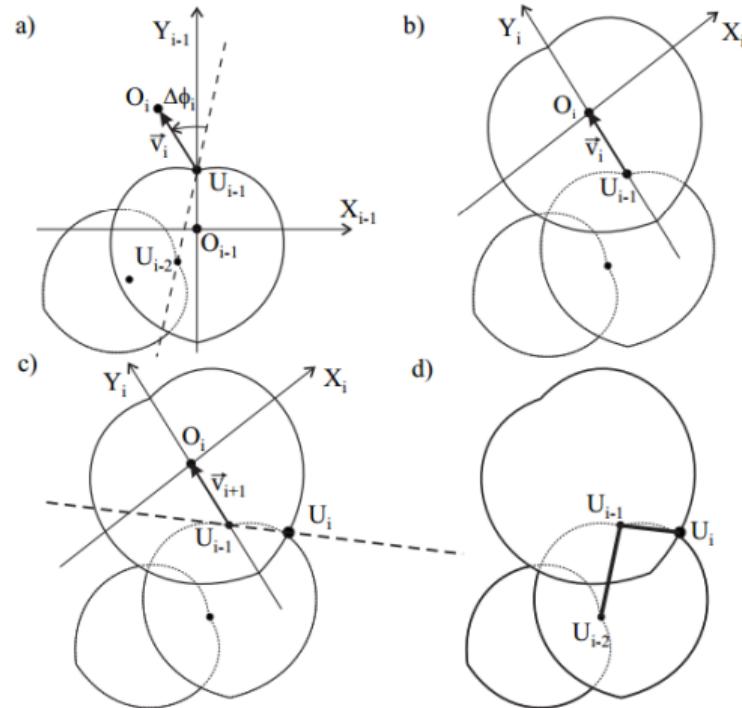
- Foraminifera
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2D and 3D numerical models of the growth of foraminiferal shells (Labaj, Topa, Tyszka, and Alda. *Computational Science*, ICCS, 2003)

# Foraminifera growth model – 2D

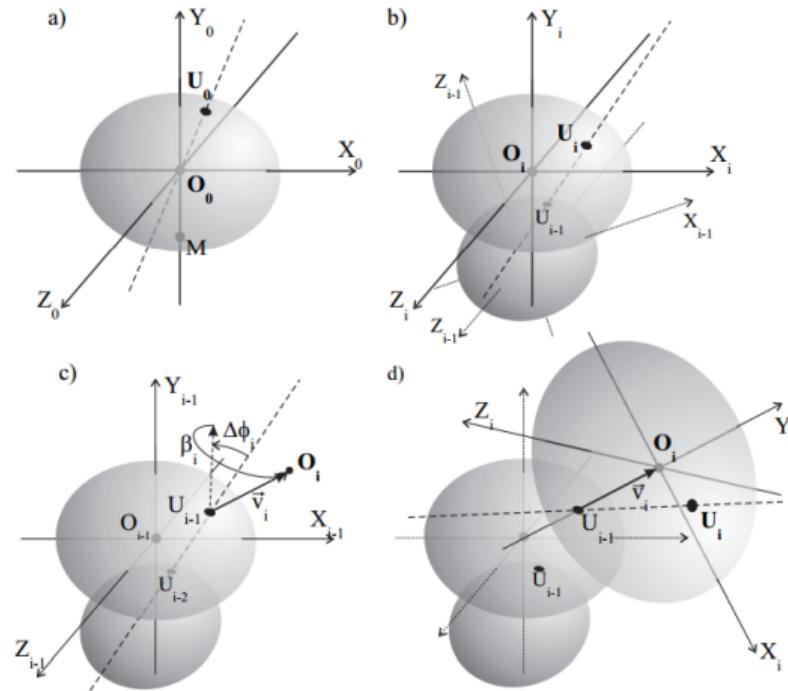
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2D and 3D numerical models of the growth of foraminiferal shells (Labaj, Topa, Tyszka, and Alda. *Computational Science, ICCS, 2003*)

# Foraminifera growth model – 3D

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2D and 3D numerical models of growth of foraminiferal shells (Labaj, Topa, Tyszka, and Alda. *Computational Science*, ICCS, 2003)

# Parameters of the model – genes

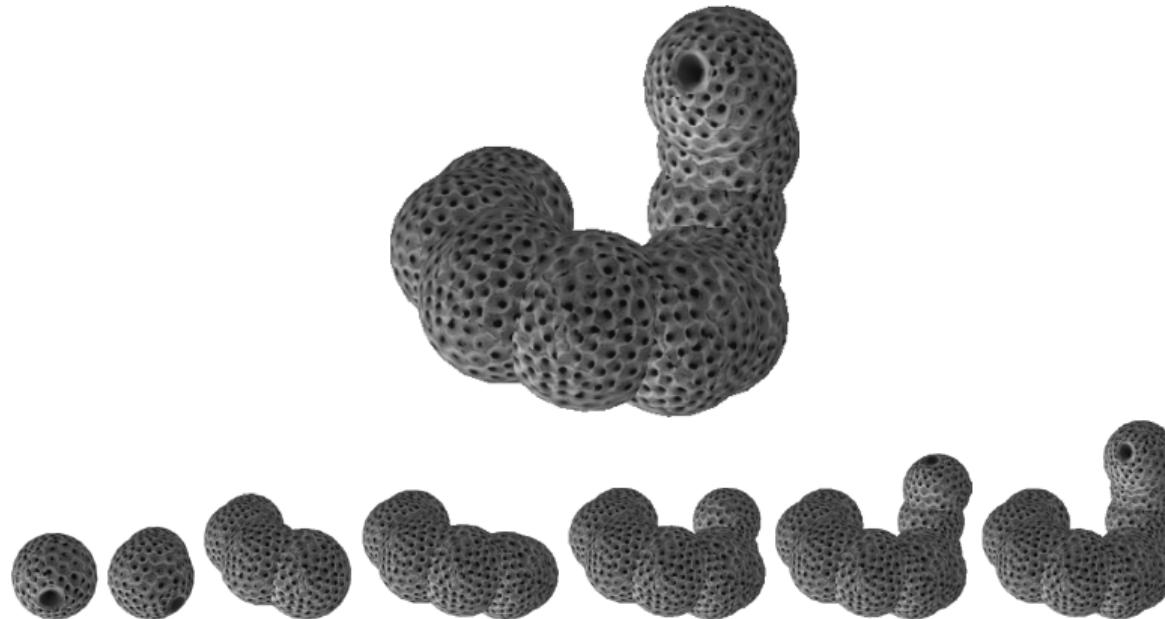
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- $N$  – number of chambers
- $K_x$  – scaling factor
- $K_y$  – scaling factor
- $K_z$  – scaling factor
- $TF$  – translation factor
- $\Delta\phi$  – deflection angle
- $\Delta\beta$  – rotation angle

# Foraminifera genotype and phenotype

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$N$	$K_x$	$K_y$	$K_z$	$TF$	$\Delta\phi$	$\Delta\beta$
10	1	1	1	-0.02	0.64	0.72



# Genotype-to-phenotype mapping analysis

Foraminifera

Genotype-to-phenotype mapping

Similarity measure

Life cycle

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References

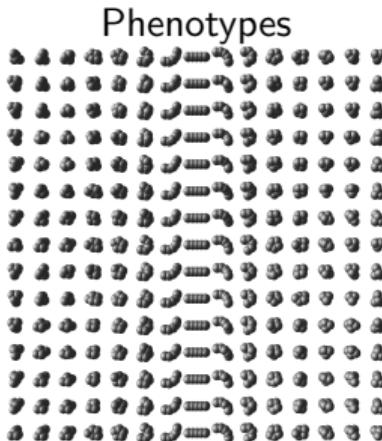
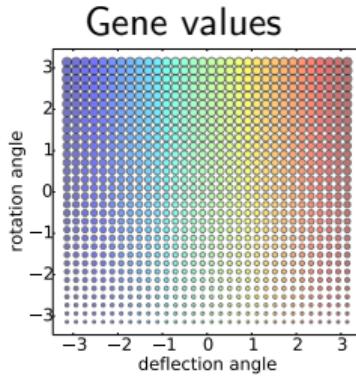
In each visualization:

- $32 \times 32$  genotypes were generated
- 5 out of 7 genes were kept constant
- 2 genes were varied

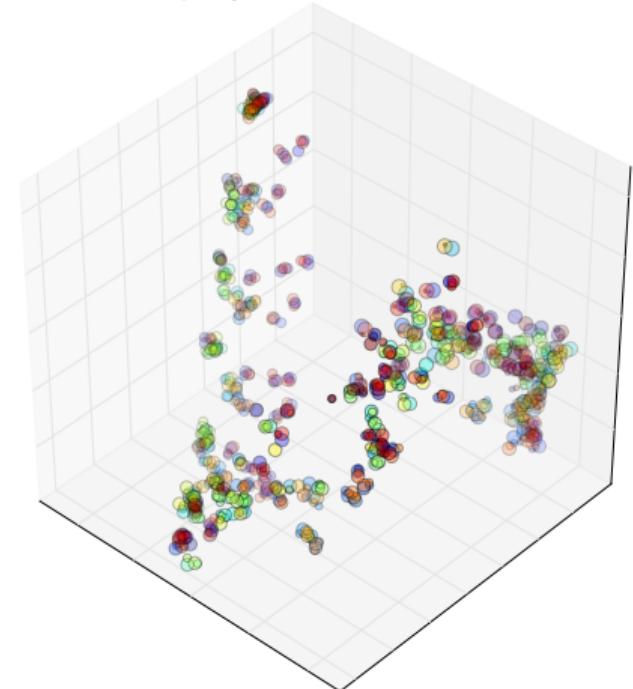
Visualization	$N$	$K_x$	$K_y$	$K_z$	$TF$	$\Delta\phi$	$\Delta\beta$
1	5	1	1	1	-0.1	$[-3.14; 3.14]$	$[-3.14; 3.14]$
2	5	1	1	1	$[-0.99; 0.99]$	$[-3.14; 3.14]$	0
3	5	1	1	1	$[-0.99; 0.99]$	0	$[-3.14; 3.14]$

# Genotype-to-phenotype mapping – $\Delta\phi$ and $\Delta\beta$

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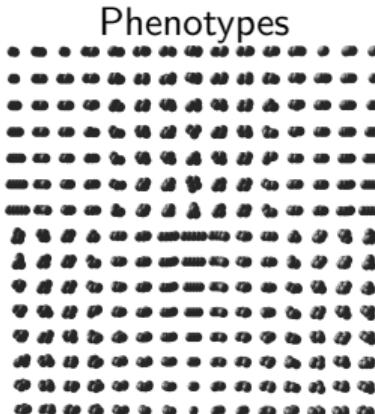
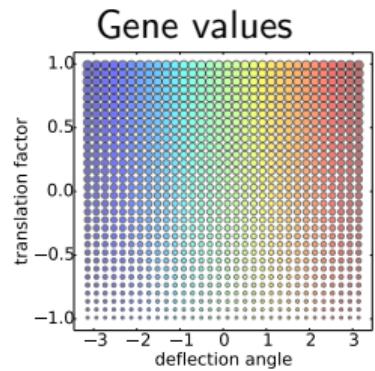


Phenotype distances  
projected into 3D

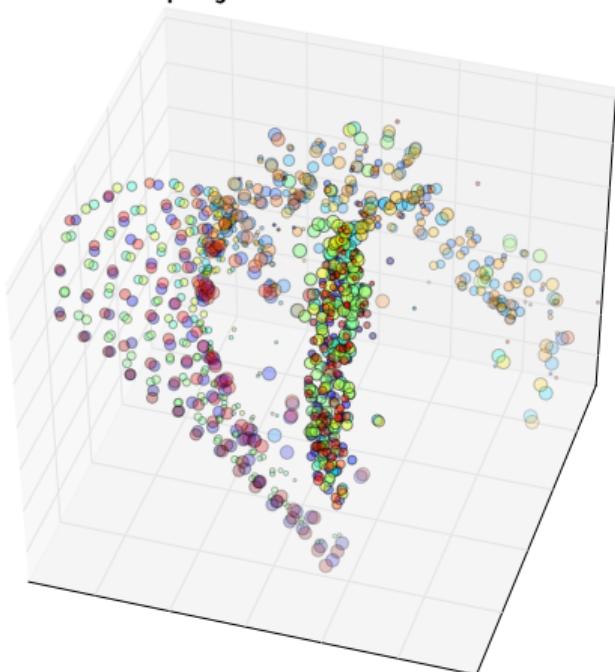


# Genotype-to-phenotype mapping – $TF$ and $\Delta\phi$

Foraminifera  
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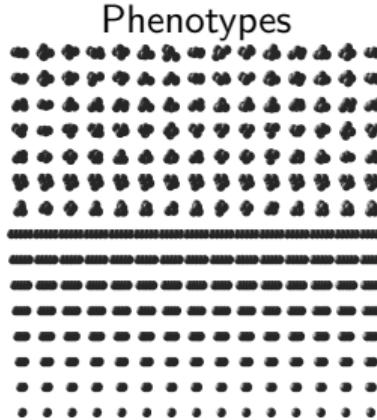
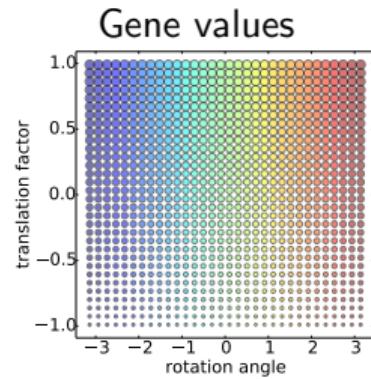


Phenotype distances projected into 3D

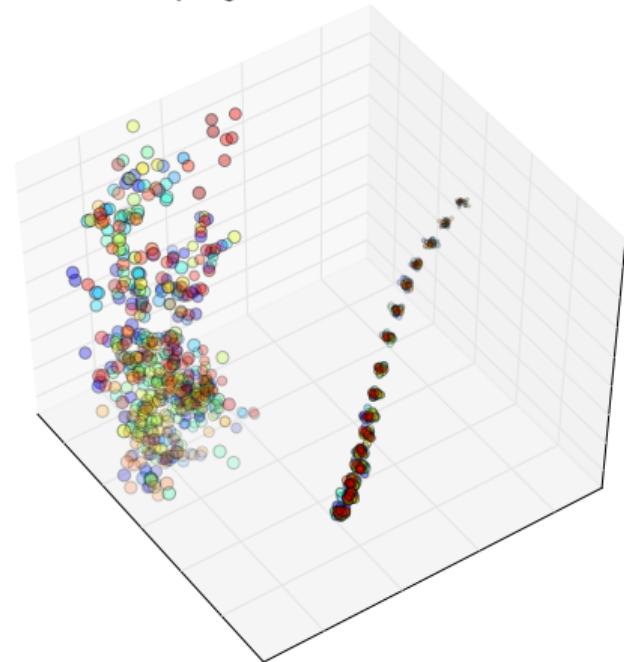


# Genotype-to-phenotype mapping – $TF$ and $\Delta\beta$

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Phenotype distances projected into 3D



# Genotype-to-phenotype mapping – summary

Foraminifera

Genotype-to-phenotype mapping

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- low *locality* of the mapping (different topologies of genetic and phenetic spaces; many discontinuities)
- discontinuities are disadvantageous from search and optimization point of view – a smooth landscape is good for evolution
- locality of biological genotype-to-phenotype mapping?

Results published in [Kom+16].

# Similarity measure

Foraminifera

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Similarity measure

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Conclusions

References

- Comparing individuals facilitates:
  - classifying morphologies
  - inferring dendrograms
  - discovering clusters
  - **phenotype-to-genotype mapping analysis**
- Other domains of application
  - computer vision
  - bioinformatics
  - chemistry

# Similarity measure – the algorithm

Foraminifera

Genotype-to-phenotype mapping

Similarity measure

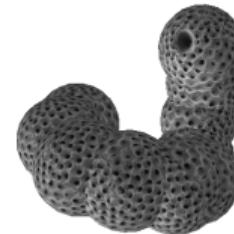
Life cycle

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Conclusions

References

- Organism model
  - Undirected graph
- Algorithm
  - Alignment of the structures
  - Construction of the matching function
  - Calculation of dissimilarity components



# Algorithm – the matching function

Foraminifera

Genotype-to-phenotype mapping

Similarity measure

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SORT( $P_i, i \in \{1, 2\}$ , descending by vertex degree)  
SORT(groups in  $P_i, i \in \{1, 2\}$  with the same vertex degree descending by *neuron\_count*)  
REPEAT  
    FIND  $U, V$  – groups of parts in  $P_1, P_2$  with the same, highest possible, degree and with parts not matched yet  
    COMPUTE  $DIST(U, V)$   
    REPEAT  
        FIND the first part  $u \in U$  which is yet unmatched  
        FIND the first part  $v \in V$  which is yet unmatched  
        FIND  $\min_{for\_u} = \min(u, V)$   
        FIND  $\min_{for\_v} = \min(v, U)$   
        MATCH( $u, \min_{for\_u}$ )  
        MATCH( $v, \min_{for\_v}$ )  
    UNTIL all parts in  $U$  or all parts in  $V$  are matched  
UNTIL all parts in the smaller set are not matched

# Dissimilarity components

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- $d_V$  – number of vertices
- $d_D$  – vertex degree
- $d_N$  – count of the neurons
- $d_G$  – geometrical distance

$$dissim = w_V * d_V + w_D * d_D + w_N * d_N + w_G * d_G$$

# Fuzzy vertex degree

Foraminifera

Genotype-to-phenotype mapping

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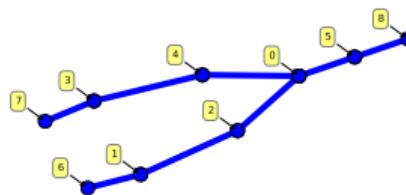
References

	0	1	2	3	4	5	6	7	8
0	0	1	0	0	0	0	0	0	0
1	1	0	1	0	0	0	0	0	0
2	0	1	0	1	0	0	1	0	0
3	0	0	1	0	1	0	0	0	0
4	0	0	0	1	0	1	0	0	0
5	0	0	0	0	1	0	0	0	0
6	0	0	1	0	0	0	0	1	0
7	0	0	0	0	0	0	1	0	1
8	0	0	0	0	0	0	0	1	0

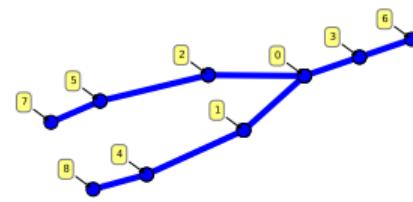
	I	II	III	IV	V	VI	VII	VII	IX
2	3.00	2.00	2.33	1.83	2.25	1.79	2.24	1.77	2.24
3	2.00	2.50	1.75	2.29	1.73	2.26	1.73	2.25	1.74
6	2.00	2.50	1.75	2.29	1.73	2.26	1.73	2.25	1.74
1	2.00	2.00	2.00	2.17	1.92	2.21	1.85	2.23	1.81
4	2.00	1.50	2.25	1.62	2.27	1.68	2.27	1.71	2.26
7	2.00	1.50	2.25	1.62	2.27	1.68	2.27	1.71	2.26
0	1.00	2.00	2.00	2.00	2.17	1.92	2.21	1.85	2.23
5	1.00	2.00	1.50	2.25	1.62	2.27	1.68	2.27	1.71
8	1.00	2.00	1.50	2.25	1.62	2.27	1.68	2.27	1.71

# Fuzzy vertex degree

- Foraminifera
- Genotype-to-phenotype mapping
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(a) Sorting by vertex degree

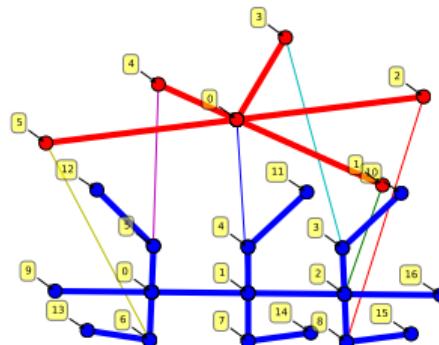


(b) Sorting by fuzzy vertex degree

# Fuzzy vertex degree

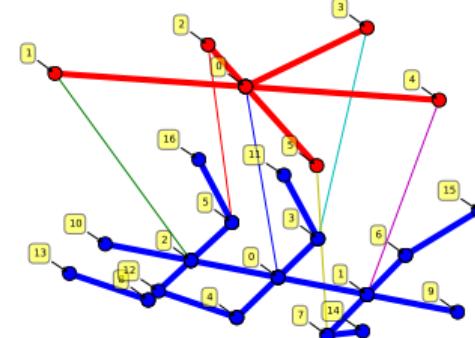
- Foraminifera
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distance=25.81



(a) Old matching

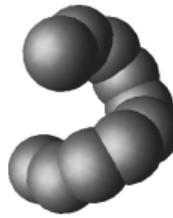
distance=24.42



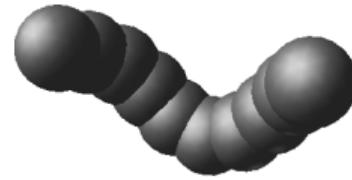
(b) New matching

# Dissimilarity matrix

Foraminifera
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(a)



(b)



(c)

	(a)	(b)	(c)
(a)	0.00	6.87	10.83
(b)	6.87	0.00	14.01
(c)	10.83	14.01	0.00

# Foraminifera reproduction cycle

- Foraminifera
- Genotype-to-phenotype mapping
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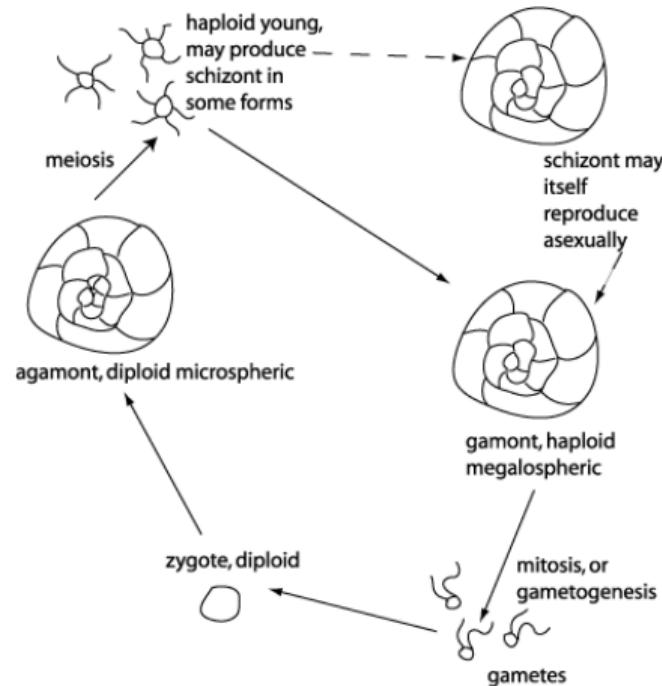
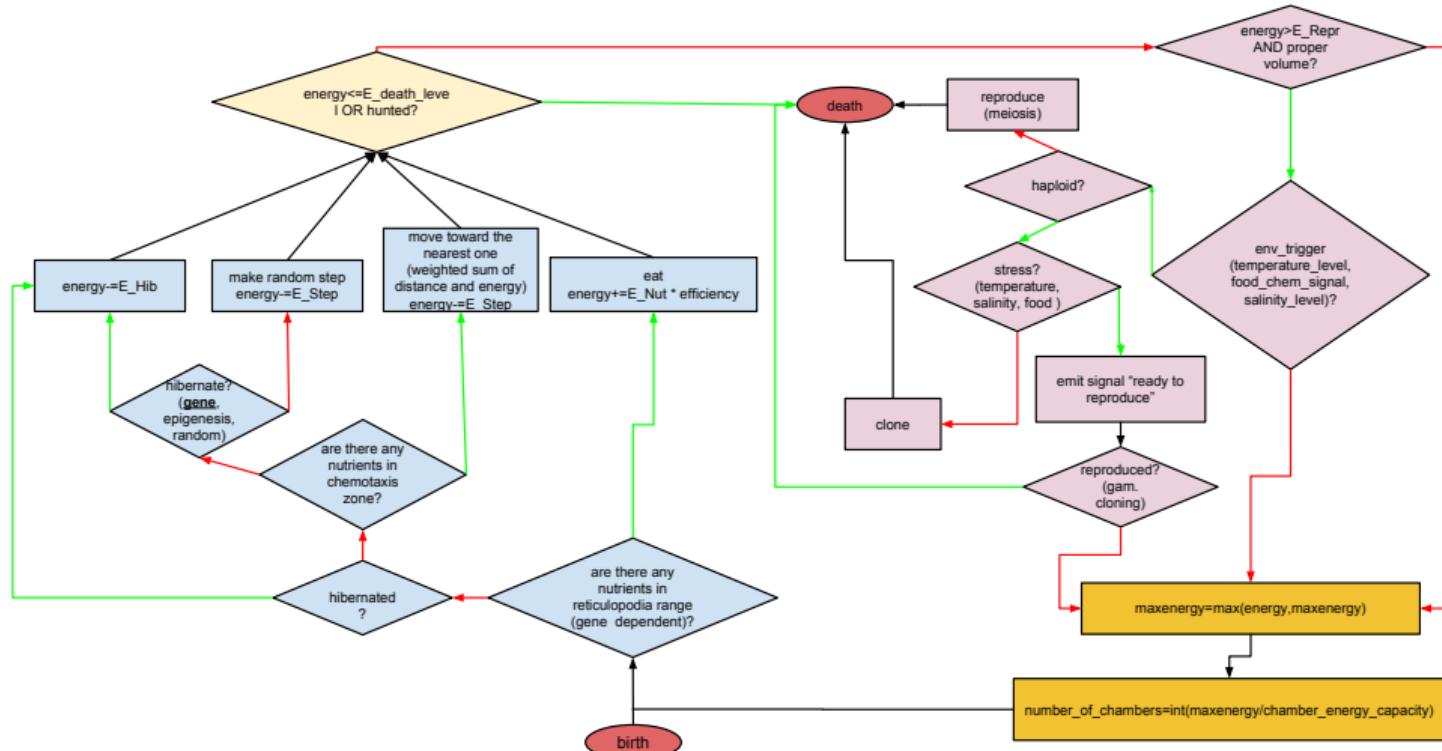


Diagram showing a generalised foraminifera life cycle note alternation between a haploid megalospheric form and a diploid microspheric form.

Redrawn from Goldstein 1999.

# Algorithm

Foraminifera  
Genotype-to-phenotype mapping  
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# Investigation of population dynamics – assumptions

Foraminifera
Genotype-to-phenotype mapping
Similarity measure
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- foraminifers and nutrients are simulated as agents
- foraminifers can actively move
- they must accumulate a sufficient amount of energy to reproduce
- haploid and diploid generations alternate
- two species with different behavioral strategies: hibernating and/or moving randomly in shortage of nutrients (food)

Experiments were performed on the eVolutus platform [[Top+16](#)].

# Population dynamics – experiments

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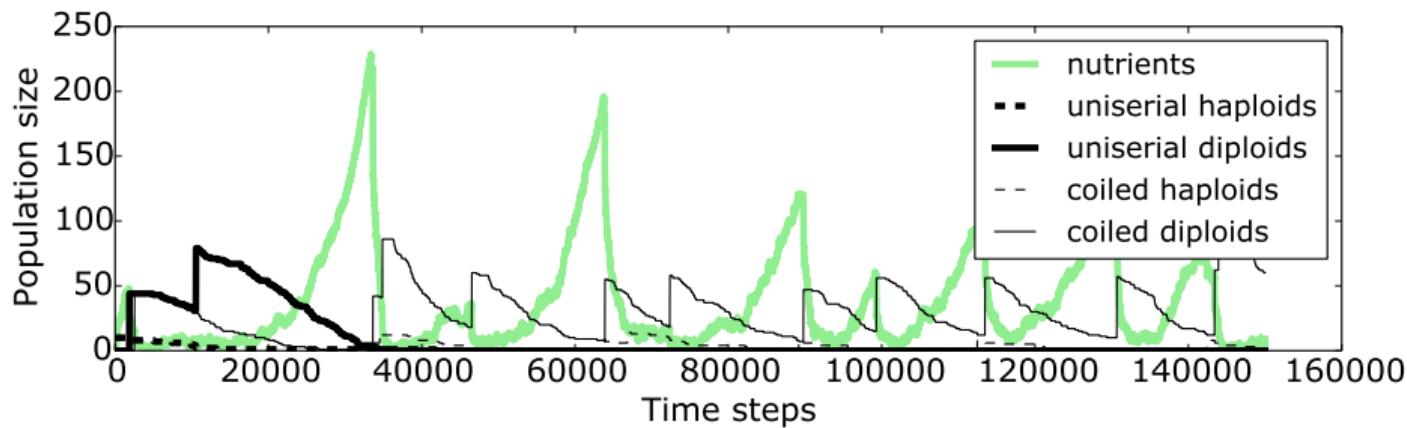
The number of runs in which a given species (moving:hibernating) survived for each combination of parameter values.

		Reticulopodia and sensing ranges [mm]	
		3,6	5,8
Feeding rate	0.05	5:0	3:2
	0.1	2:3	0:5

# Population dynamics – experiments

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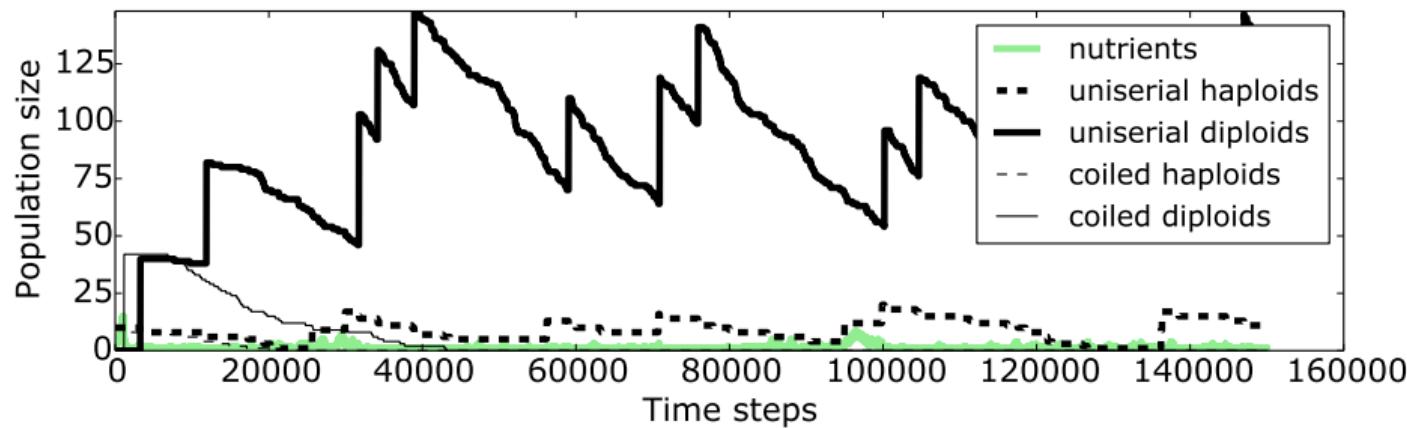
feeding rate = 0.1      ranges = 3,6



# Population dynamics – experiments

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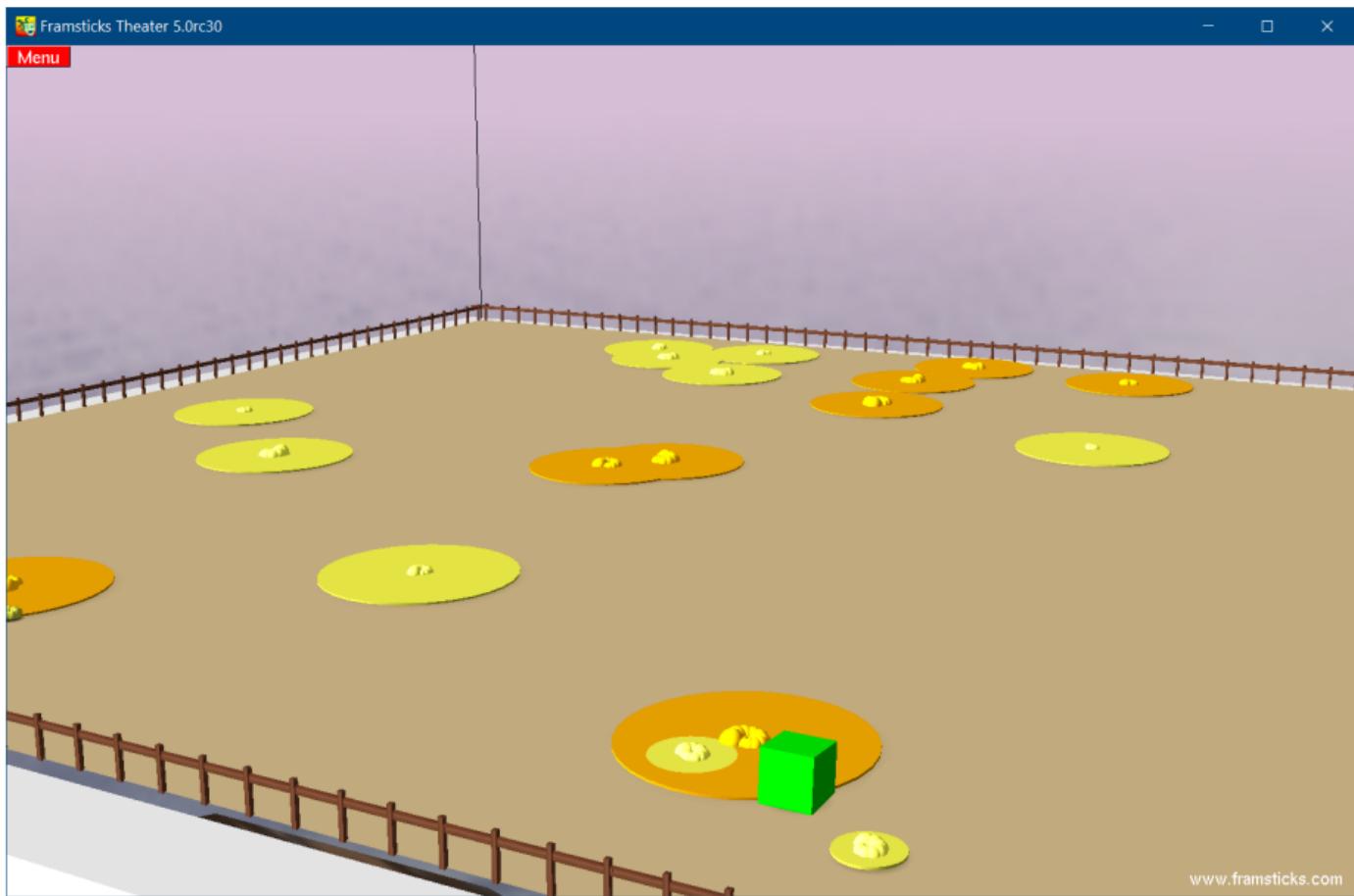
feeding rate = 0.1      ranges = 5,8



# Live demo (desktop)

<http://www.framsticks.com/foraminifera>

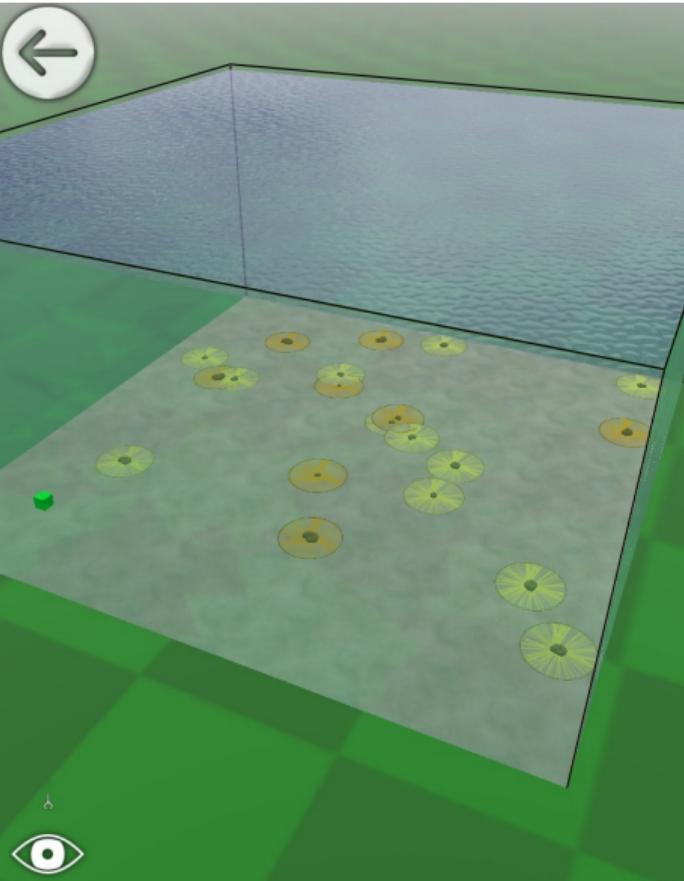
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# Live demo (mobile)

<http://www.framsticks.com/foraminifera>

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Menu  
Enhance visualization" option is enabled, reticulopodia are shown as large disks and positions of nutrients are indicated by cuboids.

More information at [www.framsticks.com/foraminifera](http://www.framsticks.com/foraminifera)

World size is 10 mm.  
Showing real-time x 2400.

Text display: Show description and status >

Speed

Paused	Very slow	Slow	Normal
Fast	Very fast		

Reload current show

Food flux

Low	Medium	High
-----	--------	------

Energy transfer per second

0.0005	0.001	0.002
--------	-------	-------

Nutrient energy [ng Corg]

=29	=109	=189
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Stress

# Conclusions

Foraminifera

Genotype-to-phenotype mapping

Similarity measure

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- Results of experiments
  - populations generally follow Lotka-Volterra dynamics
  - competition for food tends to eliminate less adapted species
  - revealed differences and discontinuities in topologies of genetic and phenetic spaces
- The model
  - initial stage of research, needs further calibration
  - integrates existing knowledge on foraminiferal physiology and ecology
  - enables testing of hypotheses on different levels and across scales
- Further work
  - development of foraminifera genetic representation
  - voxel-based similarity measure
  - comparison of similarity measures
  - development of foraminifera algorithmic model

# References I

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References

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